

# Cost-aware Defense for Parallel Server Systems against Reliability and Security Failures

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Joint work with Jiayi Wang and Li Jin, mostly done at NYU

# Security risks in network systems

- Network systems rely on data collection and transmission
  - Intelligent transportation systems (ITSs)
  - Manufacturing systems (production lines)
  - Communication networks
- Cyber components susceptible to data loss and data errors
  - E.g., traffic sensors and traffic lights can be intruded and manipulated
  - Need secure-by-design features

## Engineers who hacked into L.A. traffic signal computer, jamming streets, sentenced

DECEMBER

MIT  
Technology  
Review

[Intelligent Machines](#)

## 29 San Francisco Rail System Hacker Hacked

NOV 16

The **San Francisco Municipal Transportation Agency (SFMTA)** was hit with a **ransomware** attack on Friday, causing fare station terminals to carry the message, “You are Hacked. ALL Data Encrypted.” Turns out, the miscreant behind this extortion attempt got hacked himself this past weekend, revealing details about other victims as well as tantalizing clues about his identity and location.

## Researchers Hack Into Michigan’s Traffic Lights

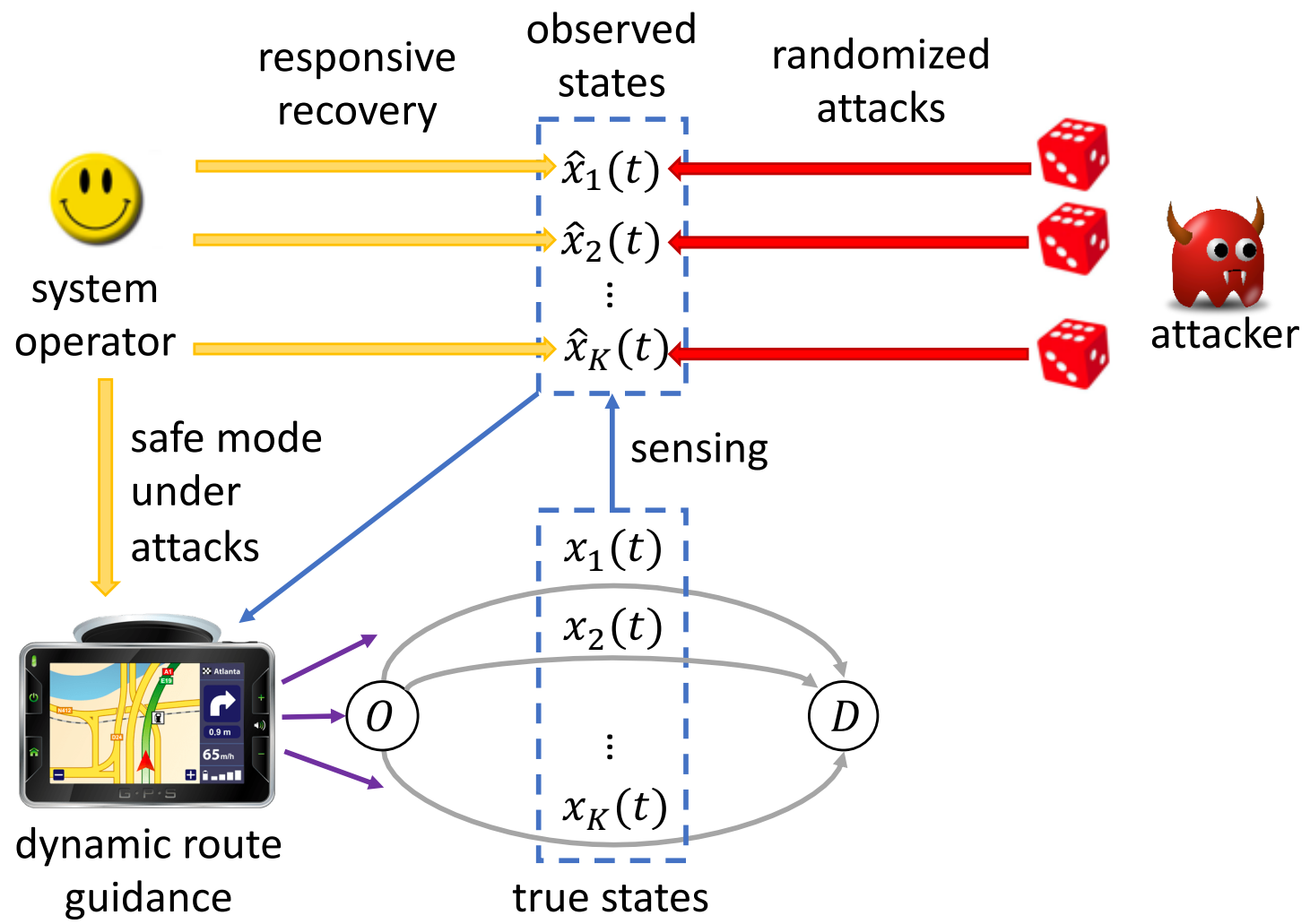
Security flaws in a system of networked stoplights point to looming problems with an increasingly connected infrastructure.



BUSINESSINSIDER.COM

An artist wheeled 99 smartphones around in a wagon to create fake traffic jams on Google Maps

# Example: dynamic routing in ITSs



# Research questions

## Modeling & analysis

- How to model stochastic & recurrent faults/attacks?
- How to quantify attacker's incentive?
- How to quantify the impact due to faults/attacks?
- How to evaluate various security risks?

## Resource allocation

- How to allocate limited/costly security resources, including redundant components, diagnosis mechanisms, etc.?

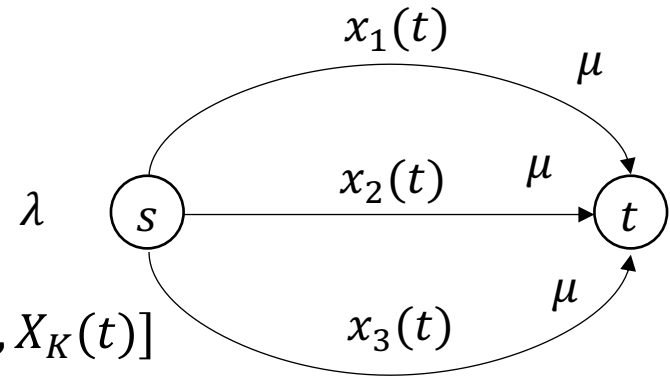
## Decision making

- How to make protecting (resp. defending) decisions in the face of random faults (resp. malicious attacks)?

# Parallel-queueing system

## Basic model

- Poisson arrivals of rate  $\lambda$
- Parallel servers with service rate  $\mu$
- State: vector of queue lengths  
$$X(t) = [X_1(t), X_2(t), \dots, X_K(t)]$$
- Dynamic routing: dynamically allocate jobs (e.g., customers, vehicles, components, data packets) to servers
- Provably optimal routing policy: join-the-shortest-queue (JSQ)<sup>[1]</sup>
- Existing works based on **perfect observation** of system state  $X(t)$  and **perfect implementation** of dynamic routing
- Faulty/failed closed-loop can be worse than open-loop (e.g., round robin or Bernoulli routing)
- Research gap: designing fault-tolerant dynamic routing



[1] Ephremides, Anthony, P. Varaiya, and Jean Walrand. "A simple dynamic routing problem." *IEEE transactions on Automatic Control* 25.4 (1980): 690-693.

# Protection against reliability failures

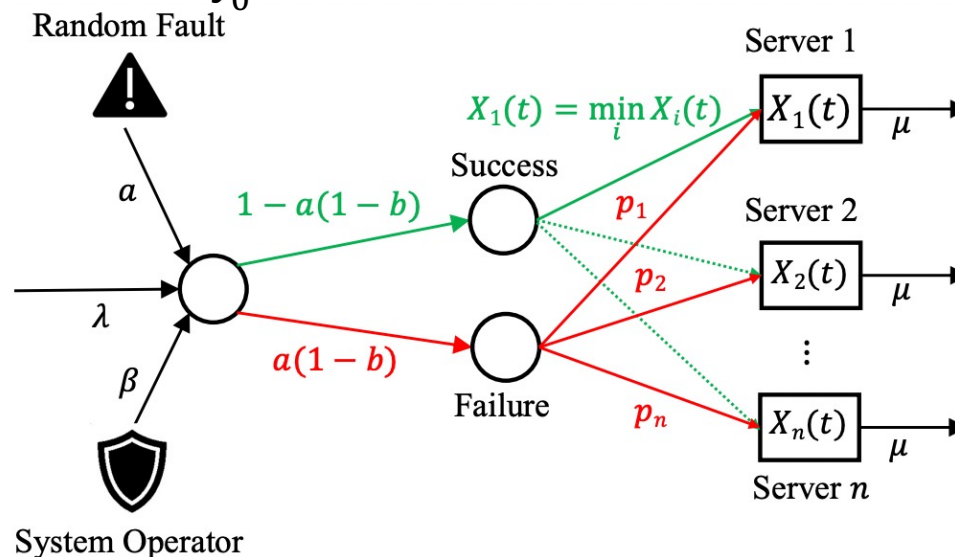
- Reliability failures

- Random malfunction: operator fails to send routing instructions
- With **constant** probability  $a$ , a job joins a random queue

- Markov decision process

- Operator protects the routing with **state-dependent** probability  $\beta(x)$
- Minimize expected cumulative discounted queuing cost + tech cost

$$J^*(x) = \min_{\beta} \mathbb{E} \left[ \int_0^{\infty} e^{-\rho t} (|X(t)| + c_b \beta(X(t))) dt \mid X(0) = x \right]$$

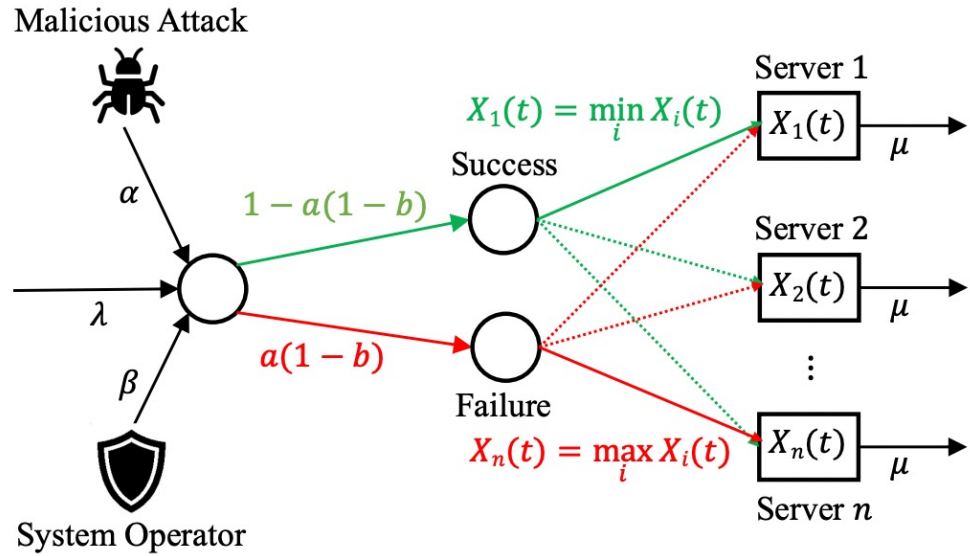


# Defense against security failures

- Security failures
  - Spoofing: attacker manipulates routing (e.g., send-to-longest-queue)
- Stochastic attacker-defender game (**attacker side**)
  - Attacker attacks with **state-dependent** probability  $\alpha(x)$
  - Maximize expected cumulative discounted **reward**

$$V_A^*(x, \beta) = \max_{\alpha} \mathbb{E} \left[ \int_0^{\infty} e^{-\rho t} R(X(t)) dt \mid X(0) = x \right]$$

$$\text{where } R(\xi) = |\xi| + c_b \beta(\xi) - c_a \alpha(\xi)$$

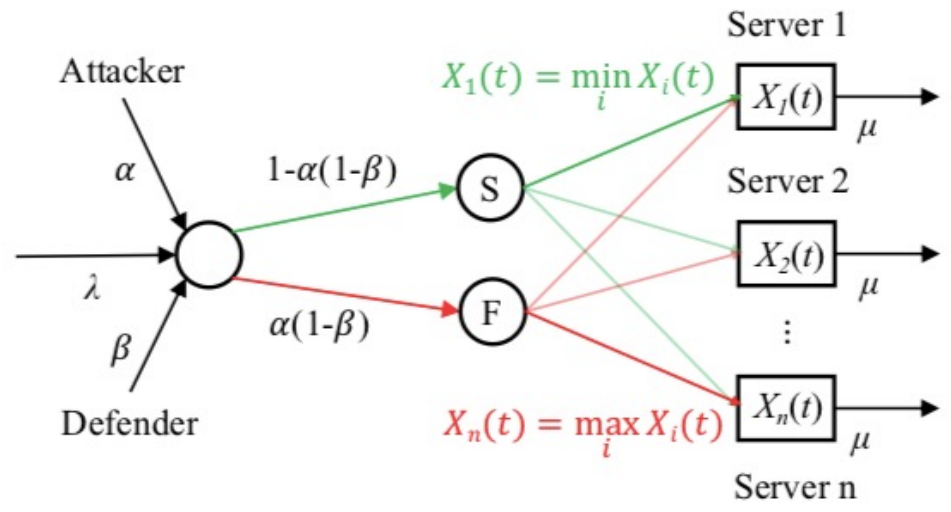


# Defense against strategic attacks (cont'd)

- Security failures
  - Routing fails iff attacked and not defended (i.e.,  $\alpha(x) = 1$  &  $\beta(x) = 0$ )
- Stochastic attacker-defender game (**operator side**)
  - Defend the routing with **state-dependent** probability  $\beta(x)$
  - Minimize expected cumulative discounted **loss**

$$V_B^*(x, \alpha) = \min_{\beta} \mathbb{E} \left[ \int_0^{\infty} e^{-\rho t} C(X(t)) dt \mid X(0) = x \right]$$

where  $C(\xi) = |\xi| + c_b \beta(\xi) - c_a \alpha(\xi)$





# Stability criteria

**Theorem 1.** The parallel n-queue system with **reliability failures** is stable if for any non-diagonal vector  $x$ ,

$$\beta(x) > 1 - \frac{\mu|x| - \lambda x_{min}}{a\lambda(\sum_{i=1}^n p_i x_i - x_{min})}.$$

**Theorem 2.** The parallel n-queue system with **security failures** is stable if for any non-diagonal vector  $x$ ,

$$\alpha(x)(1 - \beta(x)) < \frac{\mu|x| - \lambda x_{min}}{\lambda(x_{max} - x_{min})}.$$

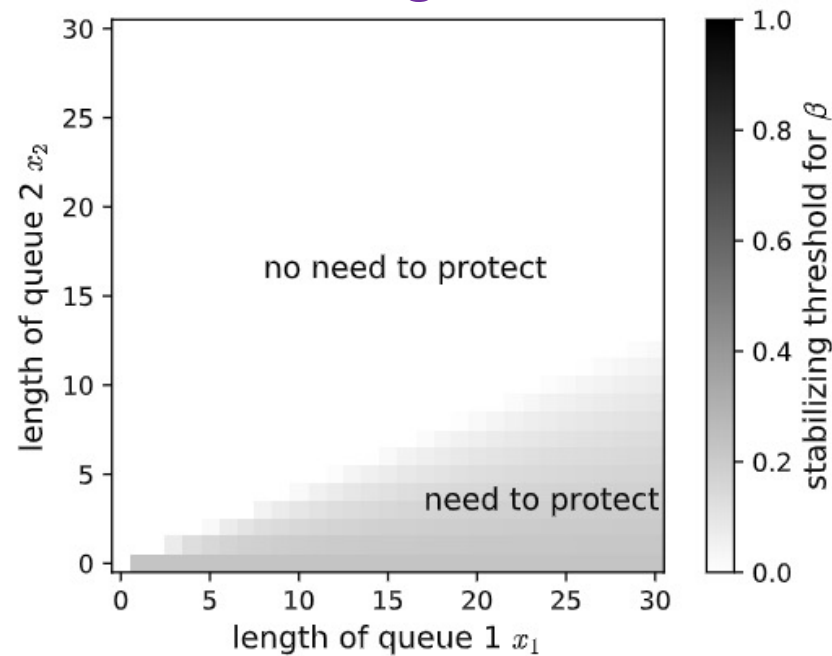
*Proof sketch.* Consider the quadratic Lyapunov function  $V(x) = \frac{1}{2} \sum_{i=1}^n x_i^2$  and apply the infinitesimal generator.

# Stability criteria (cont'd)

**Theorem 1.** The parallel n-queue system with reliability failures is stable if for any non-diagonal vector  $x$ ,

$$\beta(x) > 1 - \frac{\mu|x| - \lambda x_{min}}{a\lambda(\sum_{i=1}^n p_i x_i - x_{min})}.$$

Characterization of the stabilizing threshold:



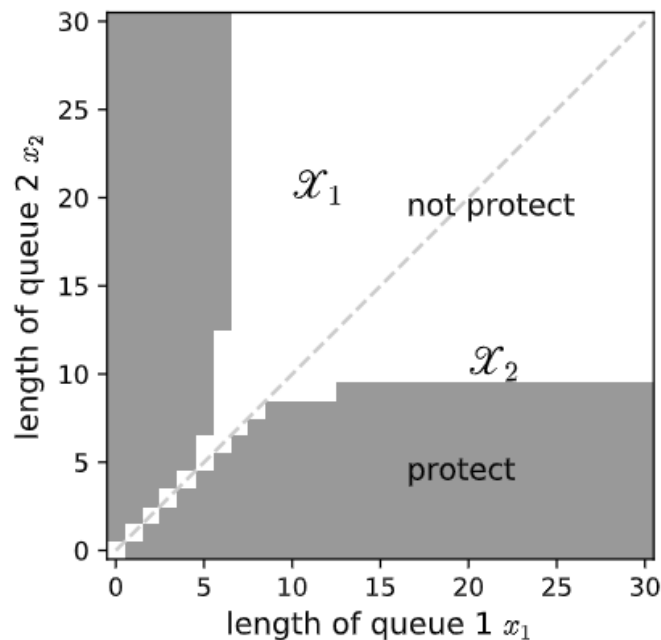
$$p_1 = 0.1, p_2 = 0.9, \lambda = 1.6, \mu = 1, a = 0.9$$

# Optimal protecting policy

**Theorem 3.** Consider a parallel n-queue system with **reliability failures**. The optimal protecting policy  $\beta^*(x)$  is **threshold-based**.

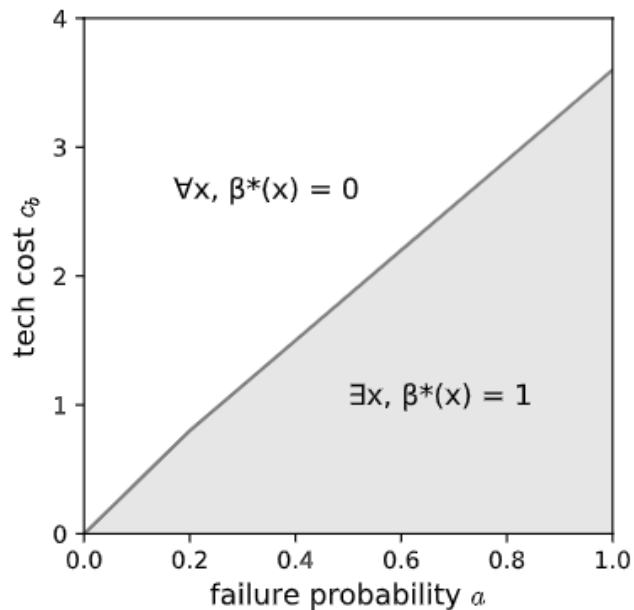
- **Bang-bang control**: operator either protects or does not protect (no probabilistic protection), i.e.,  $\beta^*(x) \in \{0,1\}$
- Operator needs to protect when 1) the queue lengths are less “balanced”; (2) the queues are close to empty

Proof idea: HJB equation and induction on value iteration.

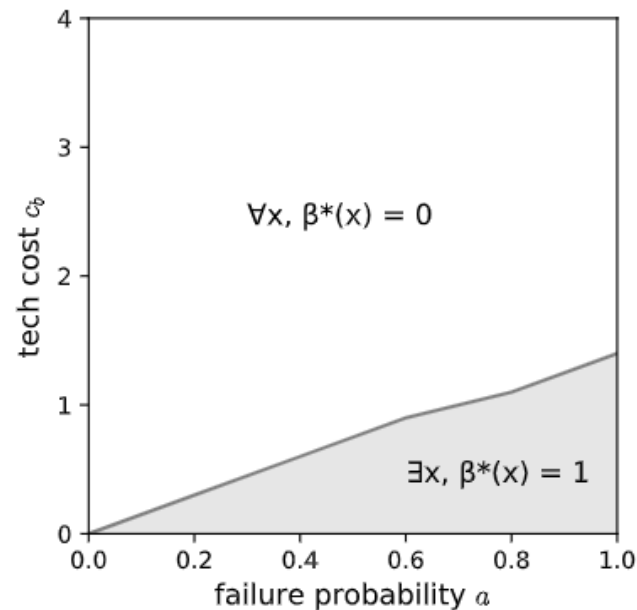


# Numerical study

The incentive to protect is non-decreasing in the failure probability  $a$ , non-increasing in the tech cost  $c_b$ , and non-decreasing in the throughput  $\lambda$  (estimation of the optimal protecting policy is based on the truncated policy iteration).



(a)  $\rho = 1.6$

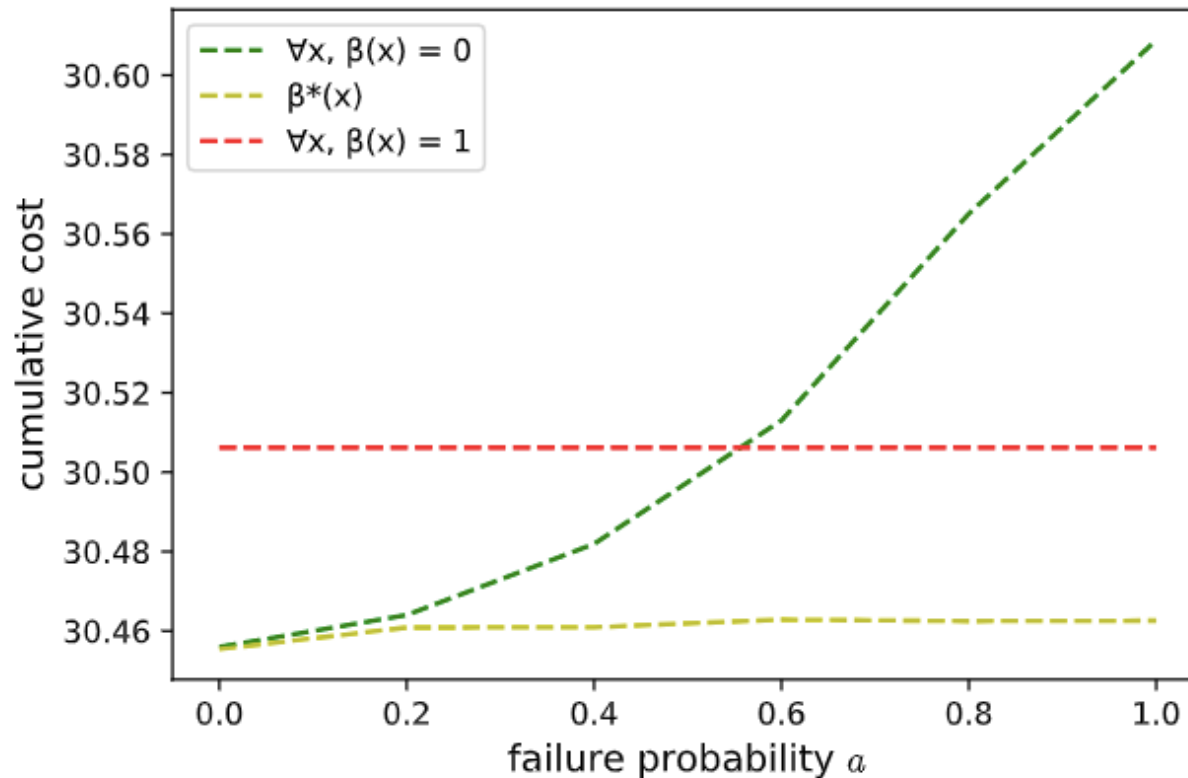


(b)  $\rho = 0.4$

Tipping points when the operator starts to protect “riskier states”

# Numerical study (cont'd)

Simulation result: the optimal **closed-loop** protecting policy  $\beta^*$  performs better in terms of the cumulative cost, compared to the **open-loop** policies (benchmark) never defend and always defend.



# Attacker-defender game

**Definition.** The equilibrium Markovian attacking (resp. defending) strategy  $\alpha^*$  (resp.  $\beta^*$ ) satisfies that for any state  $x \in \mathbb{Z}_{\geq 0}^n$ ,

$$\alpha^*(x) = \operatorname{argmax}_{\alpha} V_A^*(x, \beta^*),$$

$$\beta^*(x) = \operatorname{argmin}_{\beta} V_B^*(x, \alpha^*).$$

Attacker's (resp. defender's) is  $V_A^*(x, \beta^*)$  (resp.  $V_B^*(x, \alpha^*)$ ). In particular,  $(\alpha^*, \beta^*)$  is a **Markovian perfect equilibrium (MPE)**.

**Remark.** According to Shapley's extension on minimax theorem,

$$V_A^*(x, \beta^*) = V_B^*(x, \alpha^*) = V^*(x)$$

**Proof idea.** Induction on value iteration.

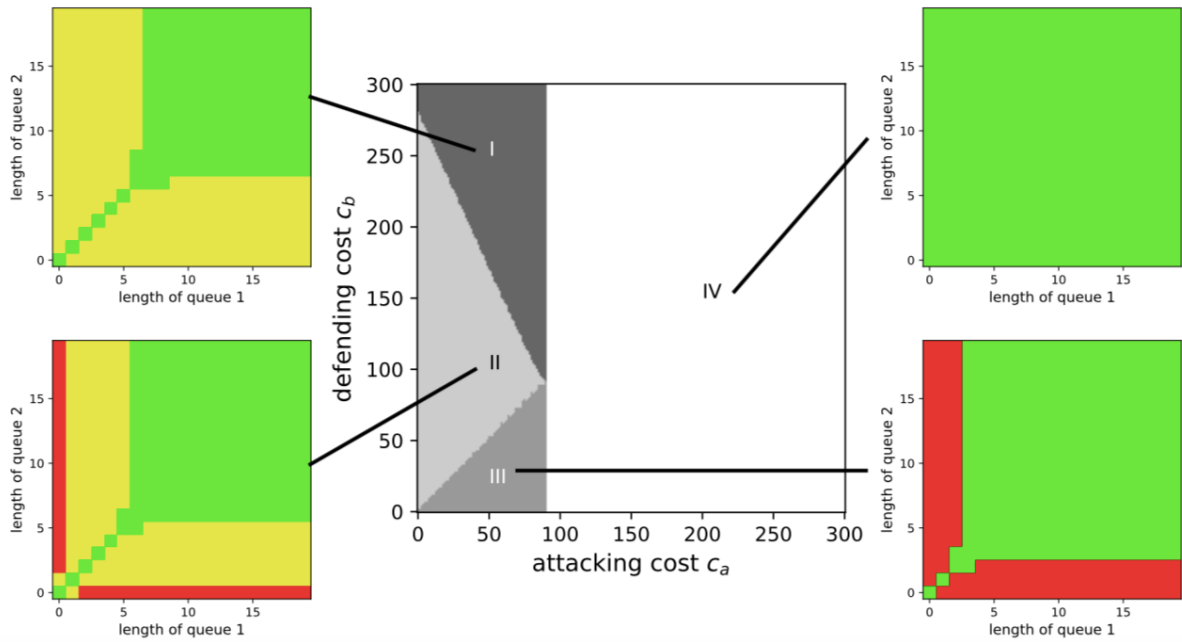
**Question.** **Existence** of MPE? - Countable infinite state space!

**Question.** **Estimation** of MPE? - Adapted Shapley's algorithm.

# MPE analysis

**Theorem 4.** The MPE has four regimes depending on  $c_a$ ,  $c_b$  and  $\delta^*(x) = \lambda(\max_j V^*(x + e_j) - \min_j V^*(x + e_j))$ . For each MPE, the state space is divided into subsets with different security risk levels:

- $S_1 = \{x | (\alpha^*(x), \beta^*(x)) = (0, 0)\}$  (low risk)
- $S_2 = \{x | (\alpha^*(x), \beta^*(x)) = (1, 0)\}$  (medium risk)
- $S_3 = \{x | (\alpha^*(x), \beta^*(x)) = (\frac{c_b}{\delta^*(x)}, 1 - \frac{c_a}{\delta^*(x)})\}$  (high risk)

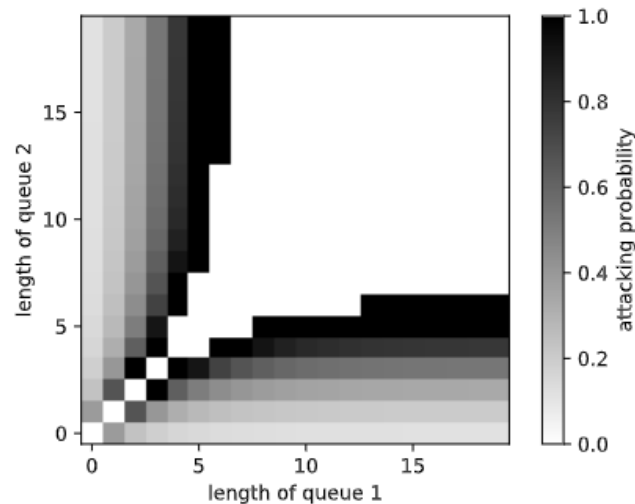


# MPE analysis (cont'd)

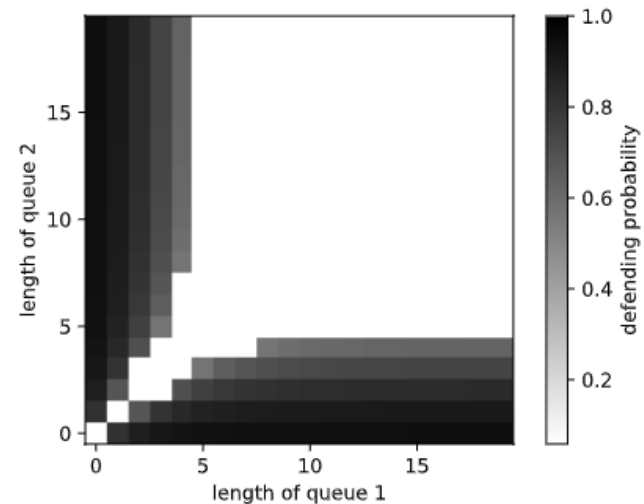
**Theorem 4.** The MPE has the following regimes depending on  $c_a$ ,  $c_b$  and  $\delta^*(x) = \lambda(\max_j V^*(x + e_j) - \min_j V^*(x + e_j))$

- $\delta^*(x) \leq c_a \Rightarrow S_1 = \{x | (\alpha^*(x), \beta^*(x)) = (0, 0)\}$  (low risk)
- $c_a < \delta^*(x) \leq c_b \Rightarrow S_2 = \{x | (\alpha^*(x), \beta^*(x)) = (1, 0)\}$  (medium risk)
- $\delta^*(x) \geq \max(c_a, c_b) > 0 \Rightarrow S_3 = \{x | (\alpha^*(x), \beta^*(x)) = (\frac{c_b}{\delta^*(x)}, 1 - \frac{c_a}{\delta^*(x)})\}$

The equilibrium strategies  $\alpha^*$ ,  $\beta^*$  are both threshold-based. (high risk)



$\alpha^*$



$\beta^*$



# Conclusion

- Without secure dynamic routing, random faults and malicious attacks can **destabilize** the queueing system
- The optimal protecting strategy and the equilibrium of attacker-defender game have **threshold-properties**
- The system operator has **higher** incentive to protect when
  - the failure probability is **higher**
  - the tech cost is **lower**
  - the throughput is **higher**
  - the queue lengths are **less “balanced”**
  - the queues are **close to empty**
- Our proposed optimal protecting policy (closed-loop) performs better than the benchmark (open-loop)
- Optimal protecting strategy (resp. equilibrium) can be estimated by truncated policy iteration (resp. adapted Shapley’s algorithm)